

This Class

4.3 Properties and  
Representations of Groups

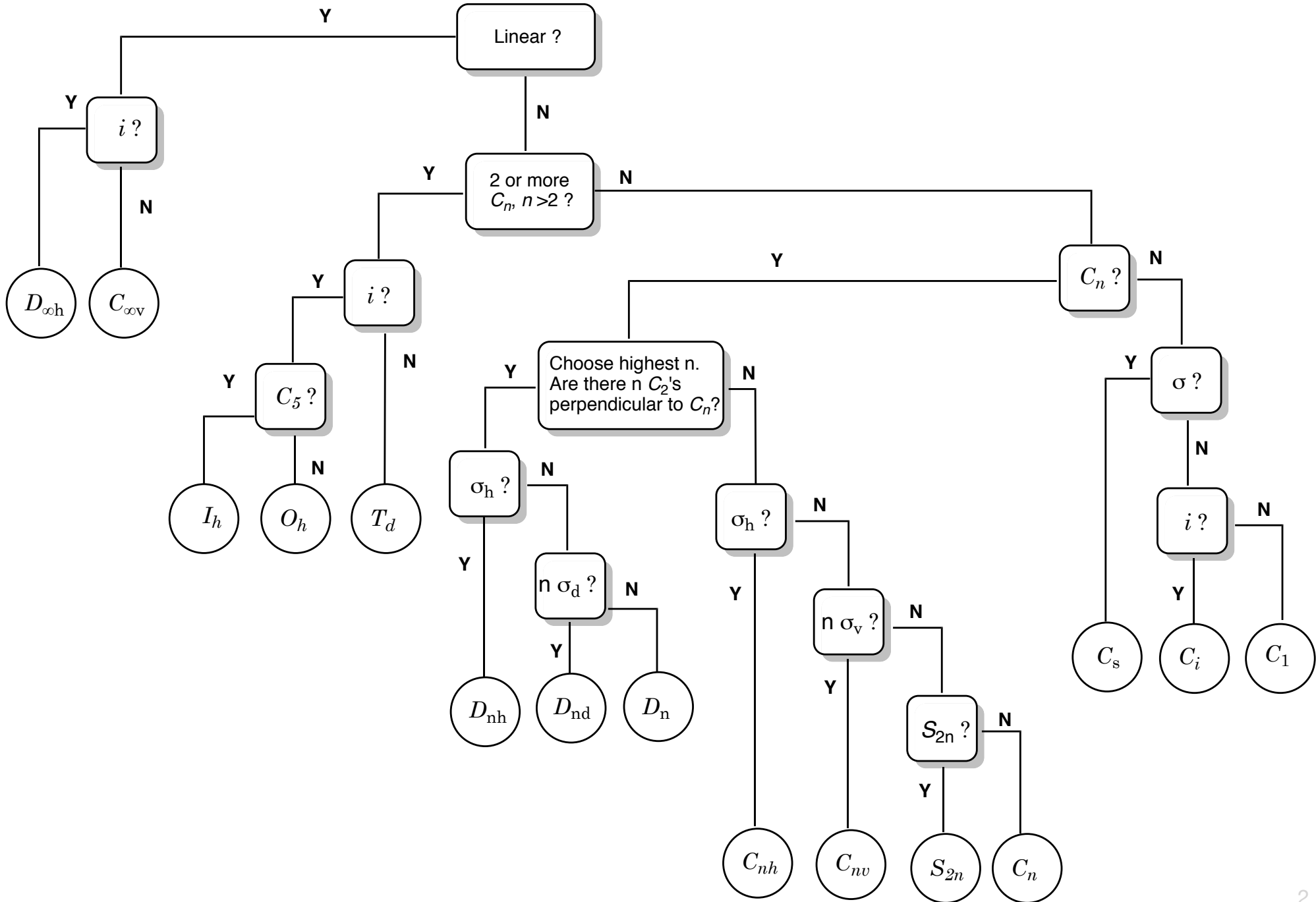
4.2

Next Class

4.4 Examples

# Using A Decision Making Tree

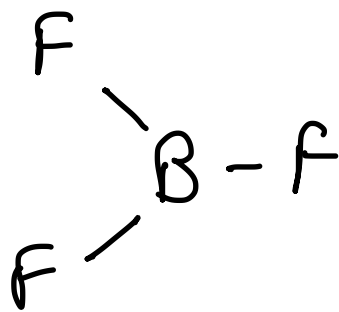
# Section 4.2



Using the Tree

Section 4.2

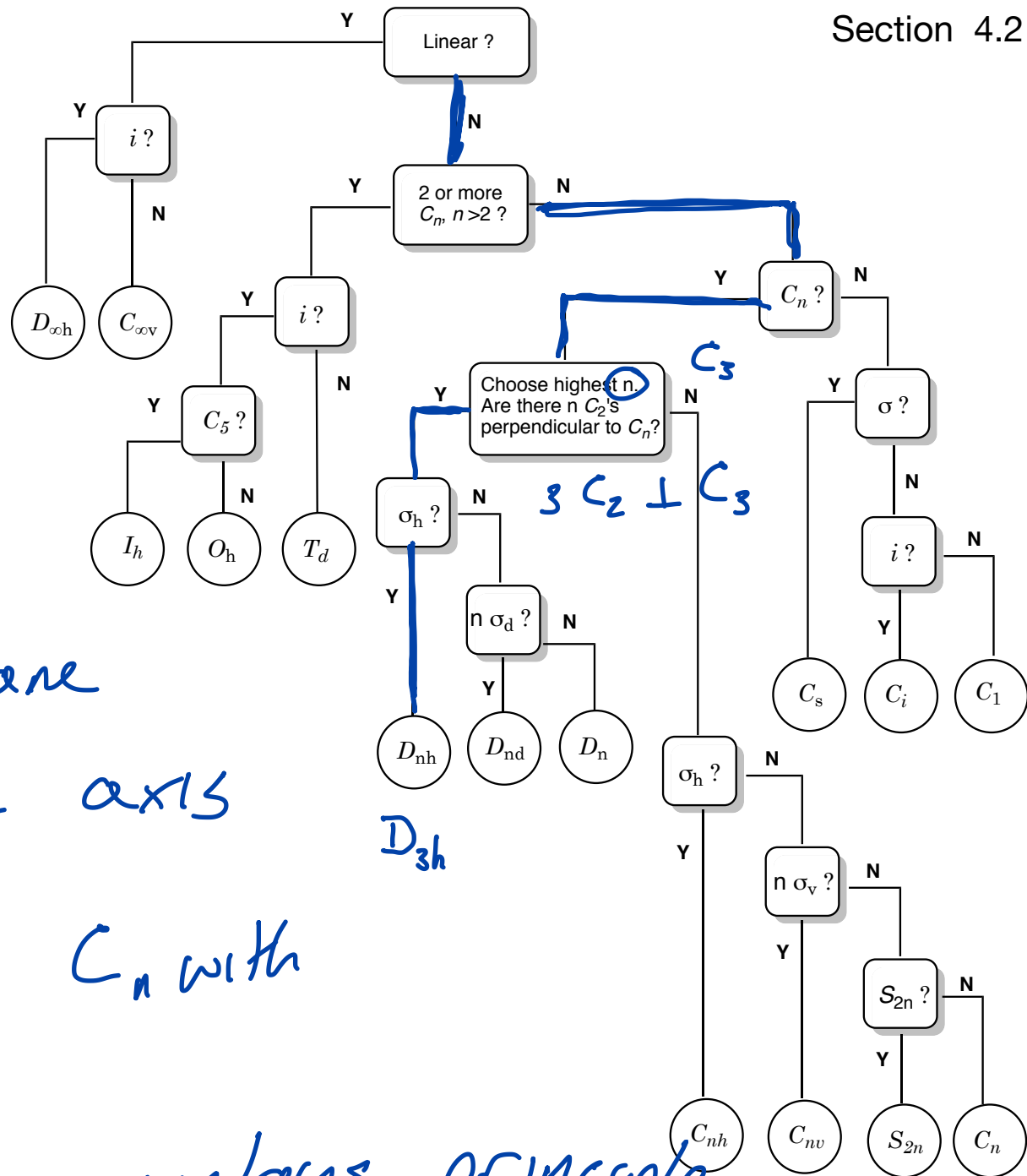
BF<sub>3</sub>



$\sigma_h$  is a mirror plane  
 ⊥ to principle axis

Principle axis is  $C_n$  with  
 highest  $n$

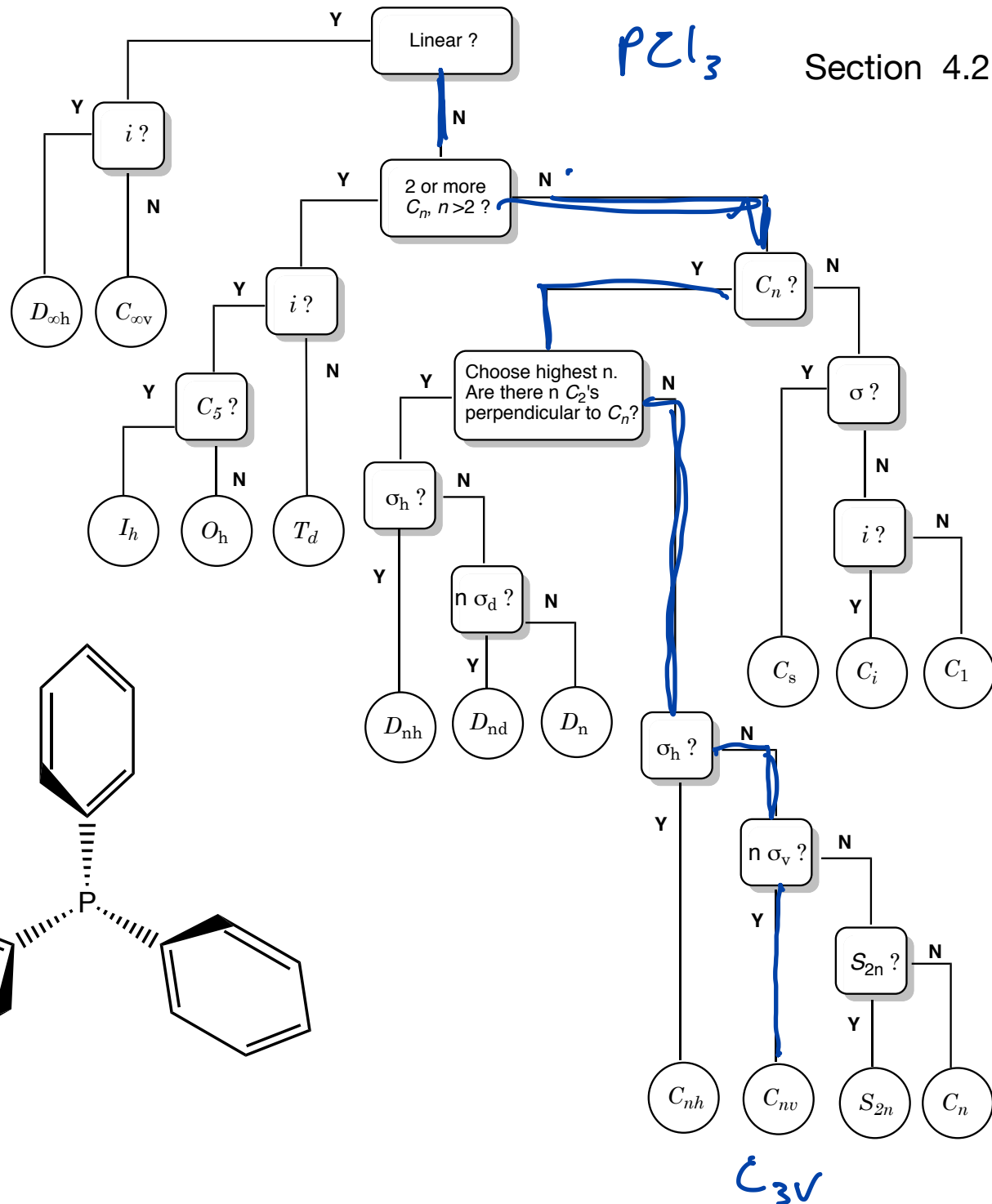
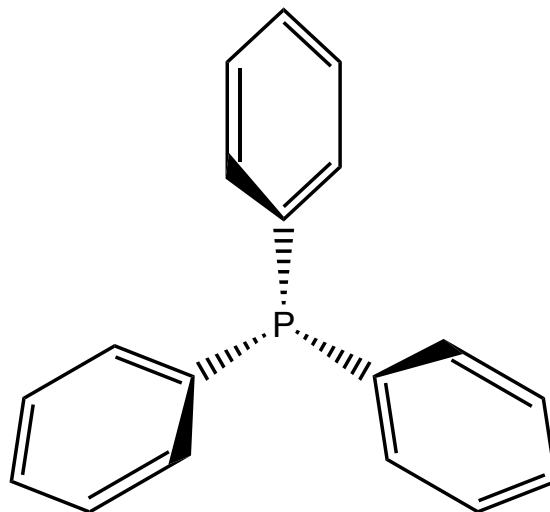
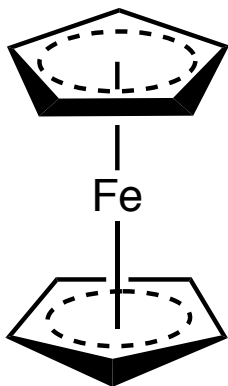
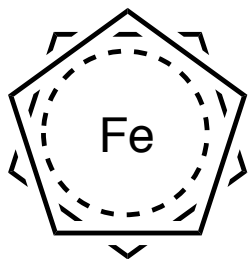
$\sigma_v$  mirror plane than contains principle axis



Practice

CH<sub>2</sub>Cl<sub>2</sub>  
 PCl<sub>3</sub>  
 HCN  
 PtCl<sub>4</sub><sup>2-</sup>  
 Fe  
 C<sub>2</sub>H<sub>2</sub>

H<sub>2</sub>O  
 BrF<sub>5</sub>  
 PPh<sub>3</sub>  
 (square planar)



$\text{CH}_2\text{Cl}_2$	$\text{C}_{2v}$	$\text{Fc}$	$\text{D}_{5d}$
$\text{PCl}_3$	$\text{C}_{3v}$	$\text{BrF}_5$	$\text{C}_{4v}$
$\text{HCN}$	$\text{C}_{\infty v}$	$\text{PPh}_3$	$\text{C}_3$
$\text{PtCl}_4^{2-}$	$\text{D}_{4h}$	$\text{H}_2\text{O}$	$\text{C}_{2v}$
$\text{C}_2\text{H}_2$	$\text{D}_{\infty h}$		

## What is a Group?

In mathematics, a group is a **set** combined with an **operation** that has the following properties

the operation combines any two elements of the set to form a third element which is part of the original set

other ways of saying this:

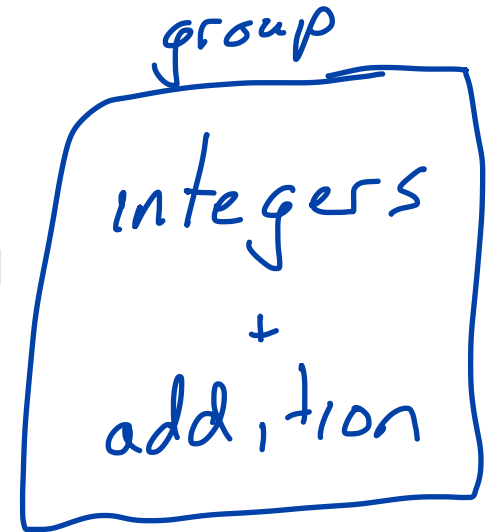
a set must be closed under the operation

there must be closure with respect to the operation

operating on elements of the set must satisfy the associative property

there must be an identity element in the set that when operated on by the operation along with any element of the set returns the original element

the operation in the set must be invertible (undoable) the set must contain elements such that the operation on two elements in the set produce the identity element



$$4 + 0 = 4$$

$$4 + -4 = 0$$

$$4 \cdot 1 = 4$$

$$4 \cdot \frac{1}{4} = 1$$

$C_{2v}$

$E$	$C_2$	$\sigma_v(xz)$	$\sigma_v(yz)$
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This is 

$C_{2v}$	E	$C_2$	$\sigma_v(xz)$	$\sigma_v(yz)$		
$A_1$	1	1	1	1	z	$x^2, y^2, z^2$
$A_2$	1	1	-1	-1	$R_z$	xy
$B_1$	1	-1	1	-1	x, $R_y$	xz
$B_2$	1	-1	-1	1	y, $R_x$	yz

these are the characters  
this is an irreducible representation



